Name:\_\_\_

This homework assignment will not be graded. It is expected that you are comfortable with the material in this assignment. This covers the entirety of Chapter 1 in the textbook. If you have questions regarding any of this, feel free to ask during office hours. When writing solutions, present your answers clearly and neatly.

## Questions you should be able to answer

- 1. What is a function? What is its domain? Its range? Give examples.
- 2. What is the graph of a real-valued function of a real variable? What is the vertical line test?
- 3. What is a piecewise-defined function? Give examples.
- 4. What are the important types of functions frequently encountered in calculus? Give an example of each type.
- 5. What is meant by an increasing function? A decreasing function? Give an example of each.
- 6. What is an even function? An odd function? What symmetry properties do the graphs of such functions have? Give an example of a function that is neither odd nor even.
- 7. If f and g are real-valued functions, how are the domains of f + g, f g, fg and f/g related to the domains of f and g?
- 8. When is it possible to compose one function with another? Does the order in which functions are composed ever matter?
- 9. How do you change the equation y = f(x) to shift its graph vertically up or down by |k| units? Horizontally to the left or right?
- 10. How do you change the equation y = f(x) to compress or stretch the graph by a factor c > 1? Reflect the graph across a coordinate axis?
- 11. Graph the six basic trigonometric functions. What symmetries do the graphs have?
- 12. What is an exponential function? What laws of exponents do they obey? How does it differ from a simple power function like  $x^n$ ? What kind of real-world phenomena are modeled by exponential functions?
- 13. What functions have inverses? How do you know if two functions f and g are inverse of one another?
- 14. How are domains, ranges and graphs of functions and their inverses related?
- 15. What is a logarithmic function? What properties does it satisfy? What is the natural logarithm function? What does the graph look like?
- 16. How are the inverse trigonometric functions defined? How can you sometimes use right triangles to find values of these functions?

## **Practice Problems**

1. Determine if whether the graph of the function is symmetric about the y-axis, the origin, or neither.

(a)  $y = x^{2/5}$ 

Answer:\_\_\_\_

(b)  $y = e^{-x^2}$ 

Answer:\_\_\_\_

Answer:\_\_\_\_\_

- 2. Determine whether the function is odd, even, or neither.
  - (a)  $y = x^5 x^3 x$

(b)  $y = x - \sin(x)$ 

(c)  $y = x \cos(x)$ 

Answer:\_\_\_\_

Answer:\_\_\_

3. If f(a - x) = f(a + x), show that g(x) := f(x + a) is even.

Answer:\_\_\_\_\_

4. Determine the domain and range of the function.

(a) 
$$y = -2 + \sqrt{1-x}$$

Answer:\_\_\_\_\_

(b)  $y = \sqrt{16 - x^2}$ 

Answer:\_\_\_

(c) $y = \ln(x - 3) + 1$	
	Answer:
5. Let $f(x) = \frac{1}{x}$ and $g(x) = \frac{1}{\sqrt{x+2}}$ . Find	
(a) $(f \circ g)(-1)$	
	Answer:
(b) $(g \circ f)(2)$	
	Answer:
(c) $(f \circ f)(x)$	
	Answer:
(d) $(g \circ g)(x)$	
	Answer:
6. Sketch the function	

(a) 
$$f(x) = \begin{cases} -x - 2, & -4 \le x \le -1 \\ -1, & -1 < x \le 1 \\ x - 2, & 1 < x \le 2 \end{cases}$$

7. Describe, in words, how each graph is obtained from the graph of y = f(x). (a) y = f(x - 5)Answer:\_\_\_ (b) y = f(4x)Answer:\_\_\_\_\_ (c) y = f(-3x)Answer:\_\_\_\_\_ (d) y = f(2x+1)Answer:\_\_\_\_\_ (e)  $y = f\left(\frac{x}{3}\right) - 4$ Answer:\_\_\_\_ (f)  $y = -3f(x) + \frac{1}{4}$ Answer:\_\_\_\_\_

8. Express the radius of a sphere as a function of the sphere's surface area. Then express the surface area as a function of volume.

Answer:\_\_\_\_\_

9. A hot air balloon rising straight up from a level field is tracked by a range finder located 500m from the point of liftoff. Express the balloon's height as a function of the angle the line from the range finder to the balloon makes with the ground.

Answer:\_\_\_\_\_

10. If Harry invests £1500 in a retirement account and earns 8% compounded annually, how long will it take this single payment to grow to £5000? If Ron invests £2000 and earns 5%, who will reach £7000 first.

Answer:\_\_\_\_